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# **Image and Video Matting: A Survey**

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**Jue Wang**

*Adobe Systems Incorporated  
801 North 34th Street  
Seattle, WA 98103  
USA*

*juewang@adobe.com*

**Michael F. Cohen**

*Microsoft Research  
One Microsoft Way  
Redmond, WA 98052  
USA*

*michael.cohen@microsoft.com*

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## Image and Video Matting: A Survey

Jue Wang<sup>1</sup> and Michael F. Cohen<sup>2</sup>

<sup>1</sup> *Adobe Systems Incorporated, 801 North 34th Street, Seattle, WA 98103, USA, [juewang@adobe.com](mailto:juewang@adobe.com)*

<sup>2</sup> *Microsoft Research, One Microsoft Way, Redmond, WA 98052, USA, [michael.cohen@microsoft.com](mailto:michael.cohen@microsoft.com)*

### Abstract

Matting refers to the problem of accurate foreground estimation in images and video. It is one of the key techniques in many image editing and film production applications, thus has been extensively studied in the literature. With the recent advances of digital cameras, using matting techniques to create novel composites or facilitate other editing tasks has gained increasing interest from both professionals as well as consumers. Consequently, various matting techniques and systems have been proposed to try to efficiently extract high quality mattes from both still images and video sequences.

This survey provides a comprehensive review of existing image and video matting algorithms and systems, with an emphasis on the advanced techniques that have been recently proposed. The first part of the survey is focused on image matting. The fundamental techniques shared by many image matting algorithms, such as color sampling methods and matting affinities, are first analyzed. Image matting techniques are then classified into three categories based on their underlying methodologies, and an objective evaluation is conducted to reveal the

advantages and disadvantages of each category. A unique Accuracy vs. Cost analysis is presented as a practical guidance for readers to properly choose matting tools that best fit their specific requirements and constraints.

The second part of the survey is focused on video matting. The difficulties and challenges of video matting are first analyzed, and various ways of combining matting algorithms with other video processing techniques for building efficient video matting systems are reviewed. Key contributions, advantages as well as limitations of important systems are summarized.

Finally, special matting systems that rely on capturing additional foreground/background information to automate the matting process are discussed. A few interesting directions for future matting research are presented in the conclusion.

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# 1

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## Introduction

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### 1.1 The Matting Problem

Extracting foreground objects from still images or video sequences plays an important role in many image and video editing applications, thus it has been extensively studied for more than 20 years. Accurately separating a foreground object from the background involves determining both full and partial pixel coverage, also known as *pulling a matte*, or *foreground matting*. This problem was mathematically established by Porter and Duff in 1984 [29]. They introduced the alpha channel as the means to control the linear interpolation of foreground and background colors for anti-aliasing purposes when rendering a foreground over an arbitrary background. Mathematically, the observed image  $I_z$  ( $z = (x, y)$ ) is modeled as a convex combination of a foreground image  $F_z$  and a background image  $B_z$  by using the alpha matte  $\alpha_z$ :

$$I_z = \alpha_z F_z + (1 - \alpha_z) B_z, \quad (1.1)$$

where  $\alpha_z$  can be any value in  $[0,1]$ . If  $\alpha_z = 1$  or  $0$ , we call pixel  $z$  *definite foreground* or *definite background*, respectively. Otherwise we call pixel  $z$  *mixed*. In most natural images, although the majority of pixels are either definite foreground or definite background, accurately

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estimating alpha values for mixed pixels is essential for fully separating the foreground from the background.

Given only a single input image, all three values  $\alpha$ ,  $F$ , and  $B$  are unknown and need to be determined at every pixel location. The known information we have for a pixel are the three dimensional color vector  $I_z$  (assuming it is represented in some 3D color space), and the unknown variables are the three dimensional color vectors  $F_z$  and  $B_z$ , and the scalar alpha value  $\alpha_z$ . Matting is thus inherently an under-constrained problem, since 7 unknown variables need to be estimated from 3 known values. Most matting approaches rely on user guidance and prior assumptions on image statistics to constrain the problem to obtain good estimates of the unknown variables. Once estimated correctly, the foreground can be seamlessly composed onto a new background, by simply replacing the original background  $B$  with a new background image  $B'$  in Equation (1.1).

### 1.2 Binary Segmentation vs. Matting

If we constrain the alpha values to be only 0 or 1 in Equation (1.1), the matting problem then degrades to another classic problem: binary image/video segmentation, where each pixel fully belongs to either foreground or background. This problem has been extensively studied since early 1960s, resulting in a large volume of related literature. Although matting is modeled as a more general problem than binary segmentation, which is theoretically harder to solve, most existing matting algorithms avoid the segmentation problem by having a *trimap* as another input in addition to the original image. The trimap may be manually specified by the user, or produced by other binary segmentation approaches. The trimap reduces the dimension of the solution space of the matting problem, and leads the matting algorithms to generate user-desired results.

Although binary segmentation and alpha matting are closely coupled problems, in this survey for image matting we will assume that a rough foreground segmentation is given, thus we mainly focus on how to accurately estimate alpha values for truly mixed pixels. We will however

discuss binary segmentation techniques in the context of video matting since they play a more central role in recent video matting systems.

### 1.3 The Trimap

Without any additional constraints, it is obvious that the total number of valid solutions to Equation (1.1) is infinite. For a trivial solution, one can set all  $\alpha_z$ s to be 1 and all  $F_z$ s to be identical to  $I_z$ s, which simply means the whole image is fully occupied by the foreground. Of course this solution is probably not consistent with what a human being will perceive from the input image. To properly extract semantically meaningful foreground objects, almost all matting approaches start by having the user segment the input image into three regions: definitely foreground  $R_f$ , definitely background  $R_b$ , and unknown  $R_u$ . This three-level pixel map is often referred to as a *trimap*. The matting problem is thus reduced to estimating  $F$ ,  $B$ , and  $\alpha$  for pixels in the unknown region based on known foreground and background regions. An example of a trimap is shown in Figure 1.1.

Instead of requiring a carefully specified trimap, some recently proposed matting approaches allow the user to specify a few foreground and background scribbles as user input to extract a matte. This intrinsically defines a very coarse trimap by marking the majority pixels (pixels have not been touched by the user) as unknowns.

One of the important factors effecting the performance of a matting algorithm is how accurate the trimap is. Ideally, the unknown region in the trimap should only cover truly mixed pixels. In other words, the unknown region around the foreground boundary should be as thin



Fig. 1.1 A matting example. From left to right: input image; user specified trimap; extracted matte; estimated foreground colors; a new composite. Results are generated by the Robust Matting algorithm [49].

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as possible to achieve the best possible matting results. This is somewhat obvious since the more accurate the trimap is, the less number of unknown variables need to be estimated, and the more known foreground and background information is available to use. However, accurately specifying a trimap requires significant amounts of user effort and is often undesirable in practice, especially for objects with large semi-transparent regions or holes. Thus a big challenge for designing a successful matting algorithm is how to achieve a good trade-off between the accuracy of the matte and the amount of the user effort required. As we will see later, different algorithms have totally different characteristics in this accuracy–efficiency space.

It is worth mentioning that the recently proposed Spectral matting algorithm [22] can automatically extract a matte from an input image without any user input. However, as the authors agreed, the automatic approach has a number of limitations including erroneous results for images with highly textured backgrounds. Thus in practice, user specified trimaps are typically necessary to achieve high quality matting results.

### 1.4 The User Interface

A properly designed user interface is critical to the success of an interactive system. Surprisingly, although the matting problem has been studied for more than two decades, very little research has been done on exploring good user interfaces for the matting task. Most of the existing matting systems work in an offline mode, where in the interactive loop, the user first specifies a trimap, that invokes matting algorithms to compute a matte. If the result is not satisfactory, the user then refines the trimap and runs the algorithm again. On the other hand, recently proposed matting algorithms mainly focus on how to improve the quality of the matte by introducing more sophisticated analysis and optimization methods, thus they are generally slow. As a result, the interactive loop described above can be very time-consuming and inefficient.

The recently proposed Soft Scissors system [46] demonstrates the possibility of a realtime matting user interface. In this system, a trimap

is created incrementally by the user with the aid of a polarized brush stroke (stroke with foreground/background boundary conditions) with dynamically updated parameters. Alpha values of pixels inside the brush stroke are computed in realtime as the user paints along the foreground edge. The instant feedback allows the user to immediately see what the foreground will look like over a new background. This approach opens many new possibilities for creating more efficient and intelligent matting user interfaces.

Another interesting image matting interface is the “components picking” interface proposed in [22]. In this approach a set of fundamental fuzzy matting components are automatically extracted from an input image, based on analyzing the smallest eigenvectors of a suitably defined Laplacian matrix. The user then selects proper components to form the foreground object using simply a few mouse clicks. However, in the case that the automatically computed components are not accurate enough, how to fine adjust the resulting matte on pixel level is unknown. One can imagine combining this approach with other matting interfaces for generating more accurate results.

Designing efficient user interfaces for video matting is certainly a more challenging task. Existing video matting interfaces can be classified into two categories: keyframe-based and volume-based approaches. Systems in the first category allow users to provide inputs on manually or automatically selected keyframes which are sparsely distributed in the input sequence, then try to automatically propagate them into intermediate frames to create a full set of constraints. Volume-based systems treat the video data as a 3D spatio-temporal video cube and allow users to directly marking pixels on extruded surfaces from the 3D cube. Details of these systems will be discussed in Section 6.

## 1.5 Matting with Extra Information

In early matting systems, the input image is often captured against a single or multiple constant-colored background(s), known as *blue screen matting*. As shown in these approaches, knowing the background greatly reduces the difficulty for extracting an accurate matte.

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For better matting results on natural images and video, special imaging systems have been designed to provide additional information or constraints to matting algorithms, such as using flash or non-flash image pairs [39], camera arrays [20], and multiple synchronized video streams [26]. Leveraging these additional sources of information, lower complexity matting algorithms can be designed to achieve fast and accurate matting. These approaches will be discussed in detail in Section 7.



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