

# Data Visualization and Health Econometrics

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## Abstract

This article reviews econometric methods for health outcomes and health care costs that are used for prediction and forecasting, risk adjustment, resource allocation, technology assessment, and policy evaluation. It focuses on the principles and practical application of data visualization and statistical graphics and how these can enhance applied econometric analysis. Particular attention is devoted to methods for skewed and heavy-tailed distributions. Practical examples show how these methods can be applied to data on individual healthcare costs and health outcomes. Topics include: an introduction to data visualization; data description and regression; generalized linear models; flexible parametric models; semiparametric models; and an application to biomarkers.

# 1

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## Introduction

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Econometric models for health outcomes and health care costs are used for prediction and forecasting in health care planning, risk adjustment by insurers and public providers of health care, geographic resource allocation, health technology assessment, and health policy impact evaluations. Methods for risk adjustment focus on predicting the treatment costs for particular types of patient, often with very large survey or administrative data sets.

Microdata for individual medical expenditures and costs of treatment are typically non-normal. Survey data often feature a spike at zero, if there are non-users in the data. Both survey and administrative data, such as registers and discharge records, typically have a heavily skewed distribution and heavy tails. The spike at zero is often modeled by a two-part specification, with a binary choice model for the probability of any costs, and a conditional regression model for the positive costs [Jones, 2000]. Due to the skewness and excess kurtosis of the data and the importance of influential observations, regression models applied directly to the raw data on the level of costs can perform poorly. Traditionally the positive observations have been transformed prior to fitting a regression model, most often by taking a logarithmic or,



sometimes, a square root transformation. Once these models have been fitted then predictions have to be retransformed back to the original — raw cost — scale. This is not straightforward to do in a robust way, especially if there is heteroskedasticity in the data on the transformed scale [Manning, 1998, Manning and Mullahy, 2001, Mullahy, 1998].

In the recent literature, attention has shifted away from linear regression models to semiparametric and flexible parametric estimators. A popular semiparametric approach is to use generalized linear models (GLMs) [e.g., Buntin and Zaslavsky, 2004, Manning and Mullahy, 2001, Manning et al., 2005, Manning, 2006]. GLMs are built around a *link function* that specifies the relationship between the conditional mean and a linear function of the covariates and a *distributional family* that specifies the form of the conditional variance as a function of the conditional mean. GLM models are estimated using a quasi-likelihood approach derived from the quasi-score or “estimating equations.”

In a conventional GLM the choice of link and distribution has to be specified a priori. In practice the most frequently used GLM specification for medical costs has been the log-link with a gamma variance [Blough et al., 1999, Manning and Mullahy, 2001, Manning et al., 2005]. Basu and Rathouz [2005] have developed a flexible semiparametric approach to the problem of selecting the appropriate link and variance functions. Their extended estimating equations estimator (EEE) approach uses a Box–Cox transformation for the link function and either a power variance or quadratic variance function for the distribution. The particular form of the link and distribution are thereby estimated from the data at hand.

Other semiparametric methods that have appeared in the literature on modeling health care costs include the conditional density estimator and finite mixture models. The conditional density approach was advocated by Gilleskie and Mroz [2004] and divides the support of the distribution of the dependent variable into discrete intervals then applies discrete hazard models to these, implemented in practice as a series of sequential logit models. Finite mixture models use a discrete mixture of parametric models and, for example, have been applied to medical

costs by [Conway and Deb \[2005\]](#). Combining simple distributions such as the gamma or log-normal in a mixture of relatively few components may approximate complex empirical distributions effectively, especially for distributions that are multimodal.

In contrast to semiparametric methods, flexible parametric methods fully specify the distribution for health care costs. Building on standard distributions such as the log-normal and gamma distributions, they move to more flexible three and four-parameter distributions such as the generalized gamma and the generalized beta distributions of the second kind (GB2). This provides the additional flexibility to fit the high level of skewness and the heavy tails seen in cost data [[Jones et al., 2014](#)]. The downside of this flexibility is a risk of over-fitting and, in practice, these approaches may be best used as a guide to selecting one of the special or limiting cases that are nested within the general models. In this respect the flexible parametric models can play a similar role to using the EEE approach to select the link and distribution functions to be used in a GLM.

Earlier literature reviews have synthesized and compared the wide range of approaches to modeling health care costs [e.g., [Hill and Miller, 2010](#), [Jones, 2000, 2011](#), [Jones et al., 2013](#), [Mullahy, 2009](#)]. In addition, studies using a quasi-Monte Carlo design, based on English administrative data for patient level costs of hospital care, have provided an assessment of the relative performance of these approaches [[Jones et al., 2014, 2015, 2016](#)]. To complement these earlier studies, this article focuses on the principles and practice of data visualization and statistical graphics and how these can enhance empirical analysis of health care costs and outcomes, especially for skewed and heavy-tailed distributions. The scope of this review is limited to non-normal but continuous outcomes such as health care costs and biomarkers. Many health economics applications deal with categorical and ordered outcomes, count data, or duration data. Methods for these are reviewed in [Jones \[2000\]](#) and [Jones et al. \[2013\]](#). The methods and applications used here are limited to cross-sectional data. For discussions of methods for panel data see [Jones \[2009\]](#) and for the use of cohort data [Von Hinke Kessler Scholder and Jones \[2015\]](#).

Practical examples show how these graphical methods can be applied using the software package Stata, which is widely used in applied econometrics. Stata is not the obvious software of choice for specialist work in data visualization especially for users who wish to present their work online and to make use of animation or interactivity. Nevertheless, for many applied econometricians it is the workhorse for data management and econometric analysis. In this article Stata code, shown in the font `courier new`, is included to show how far it is possible to go within Stata so that graphical analysis can be integrated with statistical and econometric analysis within one piece of software and using one set of syntax.

The review of methods that have been developed for health care cost regressions is complemented by an empirical case study that focuses on objectively measured health outcomes, whose distributions share many of the features of cost data. The case study applies the econometric and graphical methods to blood-based biomarkers as the dependent variables. The data set is the UK Household Longitudinal Study (UKHLS), known as Understanding Society, which is a large nationally representative longitudinal study [Benzeval et al., 2016].

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