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The Implications of Heterogeneity and Inequality for Asset Pricing

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Contents

1	Introduction and Summary	2
2	Heterogeneous Preferences, Beliefs, and Limited Participation Models	11
2.1	Heterogeneous Preferences	11
2.2	Heterogeneous Beliefs	21
2.3	Multiple Types of Agents	25
2.4	Limited Participation	27
2.5	Recursive Preferences and the Sharpe Ratio	31
2.6	Empirical Implications	33
3	Heterogeneous Endowments	37
3.1	Lack of Intra-Cohort Risk Sharing	37
3.2	Lack of Inter-Cohort Risk Sharing	45
3.3	Recursive Preferences	49
3.4	Summary and Empirical Implications	51
4	Further Applications: Equilibrium Arbitrage, Heterogeneous Stochastic Discount Factors	61
4.1	Equilibrium Arbitrage	61
4.2	Asymmetric Information and Heterogeneous Stochastic Discount Factors	64

Acknowledgements	66
Appendices	67
A Appendix	68
References	70

The Implications of Heterogeneity and Inequality for Asset Pricing

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ABSTRACT

Does heterogeneity matter for asset pricing and in particular for risk premia? Starting with an irrelevance result, I classify the literature into two groups of papers according to how they link investor heterogeneity and risk premia. The first group contains models of investors who differ in terms of their preferences, beliefs, or access to markets. Despite their differences, these models have similar implications, and can be analyzed in a unified way. The second group of papers consists of models where investors experience uninsurable income shocks. The goal of this survey is to provide one unified framework to better understand this large literature, and especially to reconcile several of the seemingly inconsistent results found in some seminal papers.

1

Introduction and Summary

Heterogeneity is all around us. Besides the obvious dimensions of heterogeneity (income and wealth), people of similar wealth and income have different savings rates and attitudes toward risk. While it is hard to argue with the existence of heterogeneity, this survey asks a question with a less obvious answer: Does heterogeneity matter for asset pricing? Specifically, does it matter for the market price of risk?

Intuitively, it would seem that the answer should be a clear yes. The savings and portfolio choices of the median retiree and a rich entrepreneur are likely to be very different. As a result, the relative wealth share of these different groups of people should matter for both interest rates and risk premia.

Yet, most leading asset-pricing models tend to be “representative” agent models, i.e., models where the distribution of wealth, income, consumption, and the associated dynamics of these quantities are all irrelevant for asset pricing.¹ One possible justification for abstracting from all distributional considerations was given in a seminal paper by Grossman and Shiller (1982). That paper revisited and substantially

¹Three leading such paradigms are Campbell and Cochrane (1999), Bansal and Yaron (2004), Barro (2006).

relaxed the assumptions of the Breeden (1979) aggregate consumption CAPM. Specifically, Grossman and Shiller (1982) showed that Breeden's aggregate-consumption CAPM continues to determine risk premia, even if risk sharing is imperfect, and therefore each consumer experiences a different consumption growth.

The argument is powerful and quite simple, since it essentially boils down to three equations. Specifically, Grossman and Shiller (1982) start with the first-order condition that if agent i is trading without frictions in some asset with (random) gross return $R_{t+\delta}$ between t and $t + \delta$ and also in the riskless asset with (certain) gross return $R_{t+\delta}^f$, then portfolio optimality requires that

$$E_t\{u'(c_{t+\delta}^i)(R_{t+\delta} - R_{t+\delta}^f)\} = 0, \quad (1.1)$$

where $u'(c_{t+\delta}^i)$ is the marginal utility of agent i . Assuming that the agent trades frequently, so that δ is small, and proceeding heuristically, a first-order expansion of $u'(c_{t+\delta}^i)$ around c_t^i gives²

$$-\frac{u'(c_t^i)}{u''(c_t^i)}E_t\{R_{t+\delta} - R_{t+\delta}^f\} \approx E_t\{(c_{t+\delta}^i - c_t^i)(R_{t+\delta} - R_{t+\delta}^f)\}. \quad (1.2)$$

Defining aggregate consumption as $C_t \equiv \int_i c_t^i di$ and integrating both sides of (1.2) across i gives

$$\begin{aligned} E_t\{R_{t+\delta} - R_{t+\delta}^f\} &\simeq \left(-\int_i \frac{u'(c_t^i)}{u''(c_t^i)} di\right)^{-1} \times E_t\{(C_{t+\delta} - C_t)(R_{t+\delta} - R_{t+\delta}^f)\} \\ &= \left(-\int_i \frac{u'(c_t^i)}{c_t^i u''(c_t^i)} \frac{c_t^i}{C_t} di\right)^{-1} \\ &\quad \times E_t\left\{\left(\frac{C_{t+\delta} - C_t}{C_t}\right)(R_{t+\delta} - R_{t+\delta}^f)\right\}. \end{aligned} \quad (1.3)$$

Equation (1.3) is remarkably similar to Breeden's aggregate consumption CAPM. It states that the excess return on an asset is given by the product of two terms. The first term is a consumption-weighted³ "harmonic average" of the relative risk aversion coefficients $-\frac{c_t^i u''(c_t^i)}{u'(c_t^i)}$

²A first-order Taylor expansion implies that $u'(c_{t+\delta}^i) \simeq u'(c_t^i) + u''(c_t^i)(c_{t+\delta}^i - c_t^i)$. Substituting this approximation into (1.1) and rearranging gives (1.2).

³The harmonic average of y_i with weights x_i is defined as $(\int_i x_i (y_i^{-1}) di)^{-1}$.

of the different investors. The second term is the expected product of *aggregate consumption growth* with the excess return.

One immediate implication of (1.3) is that even in the presence of heterogeneity, the *conditional* aggregate consumption CAPM continues to hold. Other than affecting the weights in the harmonic average of relative risk aversion, heterogeneity in *individual consumption growth rates* – whatever the reason for this heterogeneity – does not impact the risk premium. In particular, income risks that can cause idiosyncratic consumption fluctuations due to imperfect risk sharing are irrelevant for risk premia. To exaggerate for the sake of clarity, the risk premium in an economy with and without uninsurable idiosyncratic risks will be the same as long as all agents have the same risk aversion.

The Grossman and Shiller (1982) result relies on one approximation step (Equation (1.2)). This approximation step is innocuous if asset prices and consumption growth are both diffusions. Indeed, in the continuous-time limit that they consider, the approximation becomes exact, because of Ito's Lemma.

Even though the Grossman and Shiller (1982) result would appear to indicate a dead end, the almost forty years that followed its publication saw the development of a very active literature on the interactions between heterogeneity and asset pricing. Indeed, it seems that there is renewed interest in this topic in recent years because of a broader trend in macroeconomics and finance to understand the economic implications of rising income and wealth inequality.

As always happens with irrelevance results in economics (e.g., the Modigliani and Miller theorem, Ricardian equivalence, Revenue equivalence, etc.), the Grossman and Shiller (1982) result is a useful pedagogical framework for explaining how different papers in the literature “break” the irrelevance. With this in mind, in this survey I attempt a taxonomy of the different papers against the backdrop of Grossman and Shiller (1982). I classify the papers into two broad categories. The first broad category contains three strands depending on whether the source of heterogeneity is due to preferences, beliefs, or access to markets. The second broad category comprises papers on income heterogeneity and incomplete risk sharing. Within this category there are again three main strands capturing models with (lack of) intra- or inter-cohort risk

sharing and models that assume recursive preferences in a framework of imperfect risk sharing.

The first strand of the first broad category (Subsection 2.1) contains models of risk aversion heterogeneity, typically in a framework where agents have expected utility preferences. These models are not departures from Grossman and Shiller (1982), since Equation (1.3) continues to hold. Indeed, most of the papers in this literature assume that agents trade continuously and therefore Equation (1.3) is exact, not approximate. The key feature of these models is the observation that if agents have different levels of risk aversion then the consumption distribution evolves dynamically, favoring the bold in good times and the meek in bad times.

Specifically, the most interesting feature of these models is the countercyclicity of the market price of risk, or “Sharpe ratio”: because the relatively less risk-averse agents choose to be more exposed to aggregate shocks (as compared to the more risk-averse agents), a positive aggregate shock increases their wealth and consumption weight, driving down the equilibrium Sharpe ratio. By contrast, a negative shock to aggregate consumption raises the Sharpe ratio. This negative correlation between aggregate shocks and changes in the market price of risk is a prediction that these models share with the Campbell and Cochrane (1999) representative-agent model. In both types of models the aggregate consumption CAPM holds conditionally, but not unconditionally. The variations in “habits” that cause fluctuations in risk aversion in the Campbell and Cochrane (1999) model resemble the variations in the consumption weights of the heterogeneous agents in models of preference heterogeneity. As Subsection 2.3 shows, the countercyclicity of the Sharpe ratio is a remarkably robust result in models of preference heterogeneity. These models also contain interesting implications on the determination of equilibrium interest rates and bond risk premia, which are also discussed in Subsection 2.1.

The second strand of the first broad category (Subsection 2.2) comprises models of belief heterogeneity. These models assume that some investors may have different beliefs than others, possibly not resulting from superior information, but from different priors or plain irrationality. In such models, Equation (1.1) may not hold for some

investors, as they use a different expectation operator. In terms of asset-pricing implications, however, models of belief heterogeneity and preference heterogeneity are very closely related. In particular, the Sharpe ratio with heterogeneous beliefs is a consumption-weighted average of the Sharpe ratios that would obtain in homogeneous belief economies populated by only one of the constituent groups. Just as luck favors the bold in models of preference heterogeneity (in terms of increasing their wealth and consumption shares), luck favors the optimists in models of belief heterogeneity. Subsection 2.2 presents the formal connections between belief and preference heterogeneity.

The third strand of the first broad category (Subsection 2.4) comprises models where Equation (1.1) holds for some investors but not for others. For instance, if investor i is not even participating in the market for the risky asset, then Equation (1.1) does not apply to her. The implication is that when aggregating across all agents to get from Equations (1.2) to (1.3), one should only aggregate across the subset of agents that participate in the risky market. As Subsection 2.4 shows, models of this type closely resemble models of heterogeneous preferences, where non-participants are viewed as investors with infinite risk aversion for the purpose of pricing the risky assets.

Overall, the three strands of the literature mentioned so far belong to the same broad category, since they share more similarities than differences. Indeed, a novel aspect of this survey is to show that models of heterogeneous preferences, beliefs, or participation opportunities can be analyzed with similar techniques as part of one unified framework. One could go as far as argue that these models do not invalidate the core of the Grossman and Shiller (1982) result: while Equation (1.1) may fail for some of the investors, ultimately a conditional version of the aggregate consumption CAPM continues to hold, with the consumption weights acting as “conditioning variables,” to put it in the jargon used by finance econometricians.

The next broad category of papers can again be split into three strands and comprises models that assume identical investors experiencing idiosyncratic income and endowment shocks that cannot be insured due to some market failure. The papers in this group collide with a strong implication of Grossman and Shiller (1982), namely, that in any

model with diffusive (i.e., continuous) consumption and asset processes, heterogeneity should not matter in the continuous-time limit.

To be specific and give an example of this tension, one of the most influential papers in this literature is the paper by Constantinides and Duffie (1996). Using a discrete-time framework, the paper shows that a judicious specification of cross-sectional income heterogeneity allows one to support any given stochastic discount factor (in a specific class) as an equilibrium outcome. Moreover, this stochastic discount factor may differ from the one implied by the aggregate consumption CAPM. Yet, the Grossman and Shiller (1982) result would seem to allow only the stochastic discount factor implied by the aggregate consumption CAPM as an equilibrium outcome, no matter what is assumed about income heterogeneity.

It would be natural to conjecture that the discrepancy between the two papers lies in the usage of discrete- versus continuous-time methods. If true, this would be a source of concern, since it would indicate that if one were to shrink the assumed time interval in Constantinides and Duffie (1996) to zero, the results of the paper could be jeopardized.

Subsection 3.1, which discusses the first strand of the second broad category of the literature, reconciles the results of Constantinides and Duffie (1996) and Grossman and Shiller (1982). Using a minor modification of Constantinides and Duffie (1996) that allows consideration of the continuous-time limit, this subsection shows that the key insight of Constantinides and Duffie (1996) is invariant to the assumed decision interval. The results of Grossman and Shiller (1982) do not apply because the continuous-time process is not a diffusion, but a process with discontinuous sample paths. Because of this, Equation (1.2) does not hold, even in continuous time. To the best of my knowledge, this is the first paper to develop a continuous-time version of Constantinides and Duffie (1996) and provide a reconciliation between Grossman and Shiller (1982) and Constantinides and Duffie (1996).

Reconciling the results of Constantinides and Duffie (1996) and Grossman and Shiller (1982) is not just a matter of resolving a mathematical conundrum. The discussion illuminates that for income heterogeneity to matter, it has to affect the covariance between higher-order

moments of individual consumption growth and asset returns. If consumption and asset price processes are diffusions, these higher-order moments don't matter in the continuous-time limit, since Ito's Lemma implies that the marginal utility of consumption behaves (locally) like a linear function. If consumption is a discontinuous function of time, then this locally linear relation fails and higher-order moments start to matter.

Subsection 3.2 discusses the second strand of the second broad category, namely, models where the risk-sharing imperfection is not due to missing markets but rather due to missing market participants. Specifically, rather than assuming that existing cohorts cannot trade claims to their personal incomes with each other (which is the implicit market failure in models such as Constantinides and Duffie, 1996), the models in Subsection 3.2 assume that it is impossible to trade with unborn agents. This results in a lack of inter-cohort risk sharing. While starting from different assumptions and setups, the lack of either inter- or intra-cohort risk sharing implies identical stochastic discount factors.

The reason for the similarity between the two types of models is quite intuitive. The source of risk premia in models like Constantinides and Duffie (1996) is an agent's fear that if there is a large redistribution among the existing cohorts of agents, she might end up being among the losers rather than the winners. Because of risk aversion, she overweights the possibility of being among the losers and demands a risk premium for assets with bad payoffs when redistribution is high. In models of imperfect inter-cohort risk sharing investors fear that an incoming cohort of agents might introduce the next big company that will displace the companies owned by current cohorts. Therefore any assets that are prone to this displacement command a risk premium.

Subsection 3.3 discusses the third strand of the second broad category. Models in this strand make endowment heterogeneity matter by using recursive preferences rather than expected utility. In a seminal paper, Bansal and Yaron (2004) highlighted that if agents are not neutral to the timing of the resolution of uncertainty, then expected returns reflect compensation not only for short run risk, but also for risks that are associated with consumption growth in the "long run."

Mathematically, this means that Equation (1.1) does not hold and the Grossman and Shiller (1982) argument fails at its origin.

Recursive preferences alone could be an irrelevant extension if individual consumption growth is i.i.d. However, models with heterogeneous agents can easily lead to slow-moving predictable components in individual consumption growth, even if aggregate consumption growth is i.i.d. This is especially true in models where different birth cohorts experience different integrated consumption paths over their lifetime due to lack of inter-cohort risk sharing.

One interesting feature of recursive preferences is that they do not require a strong high-frequency co-movement between consumption inequality changes and asset returns to make income heterogeneity matter for the risk premium. Indeed, in the short run there need not be any relation at all, and yet income heterogeneity can matter for asset returns.

The last section of the survey (Section 4) addresses two further observations relating to Equation (1.1). Subsection 4.1 discusses models where, for each risky asset, Equation (1.1) applies only to a subset of agents. Subsection 4.2 discusses the validity of (1.1) in the presence of asymmetric information.

Subsection 4.1 discusses a multi-asset economy where all agents participate in some risky assets, but no agent participates in all asset classes. Models of this sort can feature equilibrium arbitrages. In such models it is natural to consider the incentives of agents to exploit the arbitrages by modeling pricing and participation decisions as joint outcomes. Interestingly, the presence of an arbitrage leads to nonconvexity in agents' optimization problems, which in turn leads to heterogeneous portfolio and participation decisions, even in the absence of any initial heterogeneity. In a sense, the extent of heterogeneity and equilibrium risk premia are jointly determined in response to endogenous participation decisions. Models of this sort are particularly well suited to studying portfolio flows, leverage, and asset price determination as joint outcomes.

Subsection 4.2 discusses the possibility that investors may have superior information compared to the econometrician. By itself, this is not a problem for the Grossman and Shiller (1982) argument, because

the Euler Equation (1.1) “conditions down” from the perspective of the econometrician. If, however, short-selling constraints prevent Equation (1.1) from holding for every investor and every asset, then agents may (endogenously) choose not to participate in certain asset classes. This means that the model features effectively heterogeneous stochastic discount factors. Models of this sort have important implications for portfolio biases, and performance evaluation.

In terms of presentation, this survey doesn’t simply outline these models. All subsections contain a simplified mathematical model that illustrates not only the economic ideas, but also the techniques that can be used to analyze these models. The reason for presenting these techniques is that models with heterogeneity can become intractable. One of the goals of this survey is to introduce the reader to some basic techniques to keep the mathematical structure tractable.

To be concrete, there are two difficulties when dealing with heterogeneous-agents models. The first and obvious difficulty is that the wealth distribution becomes a state variable. And second, these models tend to be nonstationary, since the innate differences between the agents lead to different consumption growth rates, which end up driving the consumption levels of different agents arbitrarily far apart in the long run.

I address these problems by placing the models within a “perpetual youth” framework. In such a framework, new generations arrive constantly with new units of the aggregate endowment. This constant flow of wealth toward each arriving cohort ensures their long-term survival. Moreover, the solution of the model boils down to the solution of a system of differential equations. However, most of the insights and the analysis don’t even require that one be able to solve these differential equations, so I relegate their formulation to the appendix.

After every subsection there is a literature review. Given the overwhelming size of the literature, the reader should view this literature review merely as providing some indicative pointers, not as an exhaustive list. It would be a mistake to presume that papers not included in the literature review are less important than the ones cited. The choice of which papers to cite was mostly dictated by the proximity of these papers to the ideas and techniques developed in each subsection.

References

- Abel, A. B. (2003). “The effects of a baby boom on stock prices and capital accumulation in the presence of social security”. *Econometrica*. 71(2): 551–578.
- Abel, A. B., J. C. Eberly, and S. Panageas (2007). “Optimal inattention to the stock market”. *American Economic Review*. 97(2): 244–249.
- Abel, A. B., J. C. Eberly, and S. Panageas (2013). “Optimal inattention to the stock market with information costs and transactions costs”. *Econometrica*. 81(4): 1455–1481.
- Alvarez, F. and U. J. Jermann (2000). “Efficiency, equilibrium, and asset pricing with risk of default”. *Econometrica*. 68(4): 775–797.
- Alvarez, F. and A. Atkeson (2018). “Random risk aversion and liquidity: A model of asset pricing and trade volumes”. *Working Paper*. University of Chicago and UCLA.
- Angeletos, G.-M. and L. Calvet (2006). “Idiosyncratic production risk, growth and the business cycle”. *Journal of Monetary Economics*. 53(6): 1095–1115.
- Aumann, R. J. (1966). “Existence of competitive equilibria in markets with a continuum of traders”. *Econometrica*. 34(1): 1–17.
- Bansal, R. and A. Yaron (2004). “Risks for the long run: A potential resolution of asset pricing puzzles”. *Journal of Finance*. 59(4): 1481–1509.

- Barro, R. J. (2006). “Rare disasters and asset markets in the twentieth century”. *Quarterly Journal of Economics*. 121(3): 823–866.
- Barro, R. J., J. Fernandez-Villaverde, O. Levintal, and A. Mollerus (2017). “Safe assets”. *Working Paper*.
- Basak, S. and D. Cuoco (1998). “An equilibrium model with restricted stock market participation”. *Review of Financial Studies*. 11(2): 309–341.
- Basak, S. and B. Croitoru (2000). “Equilibrium mispricing in a capital market with portfolio constraints”. *The Review of Financial Studies*. 13(3): 715–748.
- Bhamra, H. S. and R. Uppal (2013). “Asset prices with heterogeneity in preferences and beliefs”. *The Review of Financial Studies*. 27(2): 519–580.
- Blanchard, O. J. (1985). “Debt, deficits, and finite horizons”. *Journal of Political Economy*. 93(2): 223–247.
- Blume, L. and D. Easley (1992). “Evolution and market behavior”. *Journal of Economic Theory*. 58(1): 9–40.
- Borch, K. (1962). “Equilibrium in a reinsurance market”. *Econometrica*. 30(3): 424–444.
- Borovicka, J. (2020). “Survival and long-run dynamics with heterogeneous beliefs under recursive preferences”. *Journal of Political Economy*. 128(1): 206–251.
- Brav, A., G. M. Constantinides, and C. C. Geczy (2002). “Asset pricing with heterogeneous consumers and limited participation: Empirical evidence”. *Journal of Political Economy*. 110(4): 793–824.
- Breeden, D. T. (1979). “An intertemporal asset pricing model with stochastic consumption and investment opportunities”. *Journal of Financial Economics*. 7(3): 265–296.
- Buraschi, A. and A. Jiltsov (2006). “Model uncertainty and option markets with heterogeneous beliefs”. *The Journal of Finance*. 61(6): 2841–2897.
- Calvet, L. E., J. Y. Campbell, F. J. Gomes, and P. Sodini (2019). “The cross-section of household preferences”. *Working Paper*. Harvard University.

- Campbell, J. Y. and J. H. Cochrane (1999). “By force of habit: A consumption-based explanation of aggregate stock market behavior”. *Journal of Political Economy*. 107(2): 205–251.
- Campbell, J. Y. and Y. Nosbusch (2007). “Intergenerational risksharing and equilibrium asset prices”. *Journal of Monetary Economics*. 54(8): 2251–2268.
- Chabakauri, G. (2013). “Dynamic equilibrium with two stocks, heterogeneous investors, and portfolio constraints”. *The Review of Financial Studies*. 26(12): 3104–3141.
- Chan, Y. L. and L. Kogan (2002). “Catching up with the Joneses: Heterogeneous preferences and the dynamics of asset prices”. *Journal of Political Economy*. 110(6): 1255–1285.
- Chen, H., S. Joslin, and N.-K. Tran (2012). “Rare disasters and risk sharing with heterogeneous beliefs”. *The Review of Financial Studies*. 25(7): 2189–2224.
- Chien, Y., H. Cole, and H. Lustig (2012). “Is the volatility of the market price of risk due to intermittent portfolio rebalancing?” *American Economic Review*. 102(6): 2859–2896.
- Cogley, T. (2002). “Idiosyncratic risk and the equity premium: Evidence from the consumer expenditure survey”. *Journal of Monetary Economics*. 49(2): 309–334.
- Constantinides, G. M. and D. Duffie (1996). “Asset pricing with heterogeneous consumers”. *Journal of Political Economy*. 104(2): 219–240.
- Constantinides, G. M. and A. Ghosh (2017). “Asset pricing with countercyclical household consumption risk”. *The Journal of Finance*. 72(1): 415–460.
- Constantinides, G. M., J. B. Donaldson, and R. Mehra (2002). “Junior can’t borrow: A new perspective of the equity premium puzzle”. *Quarterly Journal of Economics*. 117(1): 269–296.
- David, A. (2008). “Heterogeneous beliefs, speculation, and the equity premium”. *The Journal of Finance*. 63(1): 41–83.
- Davilla, E. and A. Korinek (2017). “Pecuniary externalities in economies with financial frictions”. *The Review of Economic Studies*. 85(1): 352–395.

- Davilla, E. and C. Parliatore (2019). “Trading costs and informational efficiency”. *Working Paper*. Yale and New York University.
- Detemple, J. and S. Murthy (1997). “Equilibrium asset prices and no-arbitrage with portfolio constraints”. *The Review of Financial Studies*. 10(4): 1133–1174.
- Detemple, J. and A. Serrat (2003). “Dynamic equilibrium with liquidity constraints”. *The Review of Financial Studies*. 16(2): 597–629.
- Duffie, D. and L. G. Epstein (1992). “Stochastic differential utility.” *Econometrica*. 60(2): 353–394.
- Dumas, B. (1989). “Two-person dynamic equilibrium in the capital market”. *Review of Financial Studies*. 2(2): 157–188.
- Dumas, B., R. Uppal, and T. Wang (2000). “Efficient intertemporal allocations with recursive utility”. *Journal of Economic Theory*. 93(2): 240–259.
- Dumas, B., K. K. Lewis, and E. Osambela (2016). “Differences of opinion and international equity markets”. *The Review of Financial Studies*. 30(3): 750–800.
- Dybvig, P. H. and S. A. Ross (1985). “Differential information and performance measurement using a security market line”. *Journal of Finance*. 40(2): 383–399.
- Ehling, P., A. Graniero, and C. Heyerdahl-Larsen (2017). “Asset prices and portfolio choice with learning from experience”. *The Review of Economic Studies*. 85(3): 1752–1780.
- Farmer, R. E. (2018). “Pricing assets in a perpetual youth model”. *Review of Economic Dynamics*. 30: 106–124.
- Favilukis, J. (2013). “Inequality, stock market participation, and the equity premium”. *Journal of Financial Economics*. 107(3): 740–759.
- Gârleanu, N. and L. H. Pedersen (2011). “Margin-based asset pricing and deviations from the law of one price”. *The Review of Financial Studies*. 24(6): 1980–2022.
- Gârleanu, N. and S. Panageas (2015). “Young, old, conservative, and bold: The implications of heterogeneity and finite lives for asset pricing”. *Journal of Political Economy*. 123(3): 670–685.
- Gârleanu, N. and S. Panageas (2018). “Finance in a time of disruptive growth”. *Working Paper*. UC Berkeley and UCLA.

- Gârleanu, N. and S. Panageas (2019). “Heterogeneity and asset prices: A different approach”. *Working Paper*. UC Berkeley and UCLA.
- Gârleanu, N. and S. Panageas (2020). “What to expect when everyone is expecting: Self-fulfilling expectations and asset-pricing puzzles”. *Journal of Financial Economics*. Forthcoming.
- Gârleanu, N., L. Kogan, and S. Panageas (2012). “Displacement risk and asset returns”. *Journal of Financial Economics*. 105: 491–510.
- Gârleanu, N., S. Panageas, and J. Yu (2015). “Financial entanglement: A theory of incomplete integration, leverage, crashes, and contagion”. *American Economic Review*. 105(7): 1979–2010.
- Gârleanu, N., S. Panageas, and J. Yu (2020). “Impediments to financial trade: Theory and applications”. *The Review of Financial Studies*. 33(6): 2697–2727.
- Geanakoplos, J., M. Magill, and M. Quinzii (2004). “Demography and the long-run predictability of the stock market”. *Brookings Papers on Economic Activity*. 2004(1): 241–307.
- Gomes, F. and A. Michaelides (2008). “Asset pricing with limited risk sharing and heterogeneous agents”. *The Review of Financial Studies*. 21(1): 415–449.
- Gomez, M. (2017). “Asset prices and wealth inequality”. *Working Paper*. Columbia University.
- Gomez, M. (2019). “Displacement and the rise in top wealth inequality”. *Working Paper*. Columbia University.
- Greenwald, D. L., M. Lettau, and S. Ludvigson (2019). “How the wealth was won: Factors shares as market fundamentals”. *NBER Working Paper*, 25769.
- Gromb, D. and D. Vayanos (2018). “The dynamics of financially constrained arbitrage”. *The Journal of Finance*. 73(4): 1713–1750.
- Grossman, S. J. and R. J. Shiller (1982). “Consumption correlatedness and risk measurement in economies with non-traded assets and heterogeneous information”. *Journal of Financial Economics*. 10(2): 195–210.
- Guvenen, F. (2009). “A parsimonious macroeconomic model for asset pricing”. *Econometrica*. 77(6): 1711–1750.
- He, H. and H. F. Pages (1993). “Labor income, borrowing constraints, and equilibrium asset prices”. *Economic Theory*. 3(4): 663–696.

- He, H. and D. M. Modest (1995). “Market frictions and consumption-based asset pricing”. *Journal of Political Economy*. 103(1): 94–117.
- Heaton, J. and D. J. Lucas (1996). “Evaluating the effects of incomplete markets on risk sharing and asset pricing”. *Journal of Political Economy*. 104(3): 443–487.
- Hebert, B. (2019). “Externalities as arbitrage”. *Working Paper*. Stanford Graduate School of Business.
- Hugonnier, J. (2012). “Rational asset pricing bubbles and portfolio constraints”. *Journal of Economic Theory*. 147(6): 2260–2302.
- Kacperczyk, M., J. Nosal, and L. Stevens (2019). “Investor sophistication and capital income inequality”. *Journal of Monetary Economics*. 107: 18–31.
- Kargar, M. (2018). “Heterogeneous intermediary asset pricing”. *Working Paper*. UCLA.
- Khorrani, P. (2019a). “Entry and slow-moving capital: Using asset markets to infer the costs of risk concentration”. *Working Paper*. University of Chicago.
- Khorrani, P. (2019b). “The risk of risk-sharing: Diversification and boom-bust cycles”. *Working Paper*. University of Chicago.
- Kocherlakota, N. R. and L. Pistaferri (2009). “Asset pricing implications of Pareto optimality with private information”. *Journal of Political Economy*. 117(3): 555–590.
- Kogan, L., S. A. Ross, J. Wang, and M. M. Westerfield (2006). “The price impact and survival of irrational traders”. *The Journal of Finance*. 61(1): 195–229.
- Kogan, L., D. Papanikolaou, and N. Stoffman (2020). “Left behind: Creative destruction, inequality, and the stock market”. *Journal of Political Economy*. 128(3): 855–906.
- Kondor, P. (2009). “Risk in dynamic arbitrage: The price effects of convergence trading”. *The Journal of Finance*. 64(2): 631–655.
- Kondor, P. and D. Vayanos (2019). “Liquidity risk and the dynamics of arbitrage capital”. *The Journal of Finance*. 74(3): 1139–1173.
- Krueger, D. and F. Kubler (2006). “Pareto-improving social security reform when financial markets are incomplete!?” *American Economic Review*. 96(3): 737–755.

- Krueger, D. and H. Lustig (2010). “When is market incompleteness irrelevant for the price of aggregate risk (and when is it not)?” *Journal of Economic Theory*. 145(1): 1–41.
- Liu, J. and F. A. Longstaff (2003). “Losing money on arbitrage: Optimal dynamic portfolio choice in markets with arbitrage opportunities”. *The Review of Financial Studies*. 17(3): 611–641.
- Longstaff, F. A. and J. Wang (2012). “Asset pricing and the credit market”. *The Review of Financial Studies*. 25(11): 3169–3215.
- Lucas, D. (1994). “Asset pricing with undiversifiable income risk and short sales constraints: Deepening the equity premium puzzle”. *Journal of Monetary Economics*. 34(3): 325–341.
- Luttmer, E. (1996). “Asset pricing in economies with frictions”. *Econometrica*. 64(6): 1439–1467.
- Mankiw, N. (1986). “The equity premium and the concentration of aggregate shocks”. *Journal of Financial Economics*. 17(1): 211–219.
- Mankiw, N. and S. P. Zeldes (1991). “The consumption of stockholders and nonstockholders”. *Journal of Financial Economics*. 29(1): 97–112.
- Marcet, A. and R. Marimon (1998). “Recursive contracts”. *Working Paper*.
- Maurer, T. (2017). “Asset pricing implications of demographic change”. *Working Paper*. Washington University in St. Louis.
- Mayers, D. and E. Rice (1979). “Measuring portfolio performance and the empirical content of asset pricing models”. *Journal of Financial Economics*. 7(1): 3–28.
- Parker, J. A. and A. Vissing-Jorgensen (2009). “Who bears aggregate fluctuations and how?” *American Economic Review*. 99(2): 399–405.
- Pastor, L. and P. Veronesi (2019). “Inequality aversion, populism, and the backlash against globalization”. *Working Paper*. University of Chicago.
- Sandroni, A. (2000). “Do markets favor agents able to make accurate predictions?” *Econometrica*. 68(6): 1303–1341.
- Santos, T. and P. Veronesi (2018). “Leverage”. *NBER Working Paper 22905*.
- Scheinkman, J. and W. Xiong (2003). “Overconfidence and speculative bubbles”. *Journal of Political Economy*. 111(6): 1183–1220.

- Schmidt, L. D. W. (2015). “Climbing and falling off the ladder: Asset pricing implications of labor market event risk”. *Working Paper*. MIT Sloan.
- Schneider, A. (2017). “Risk sharing and the term structure of interest rates”. *Working Paper*. Federal Reserve Board of Governors.
- Storesletten, K., C. Telmer, and A. Yaron (2004). “Cyclical dynamics in idiosyncratic labor market risk”. *Journal of Political Economy*. 112(3): 695–717.
- Storesletten, K., C. I. Telmer, and A. Yaron (2007). “Asset pricing with idiosyncratic risk and overlapping generations”. *Review of Economic Dynamics*. 10(4): 519–548.
- Telmer, C. I. (1993). “Asset-pricing puzzles and incomplete markets”. *The Journal of Finance*. 48(5): 1803–1832.
- Toda, A. A. and K. Walsh (2020). “The equity premium and the one percent”. *The Review of Financial Studies*. 33(8): 3583–3623.
- Vissing-Jorgensen, A. (2002). “Limited asset market participation and the elasticity of intertemporal substitution”. *Journal of Political Economy*. 110(4): 825–853.
- Wang, J. (1996). “The term structure of interest rates in a pure exchange economy with heterogeneous investors”. *Journal of Financial Economics*. 41(1): 75–110.
- Xiouros, C. and F. Zapatero (2010). “The representative agent of an economy with external habit formation and heterogeneous risk aversion”. *The Review of Financial Studies*. 23(8): 3017–3047.
- Yan, H. (2008). “Natural selection in financial markets: Does it work?” *Management Science*. 54(11): 1935–1950.
- Zentefis, A. (2019a). “Bank net worth and frustrated monetary policy”. *Working Paper*. Yale School of Management.
- Zentefis, A. (2019b). “Self-fulfilling asset prices”. *Working Paper*. Yale School of Management.
- Zheng, G. (2019). “Wealth shares in the long run”. *Working Paper*. UCLA.