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# **Energy-Efficient Time-Domain Computation for Edge Devices: Challenges and Prospects**

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# **Energy-Efficient Time-Domain Computation for Edge Devices: Challenges and Prospects**

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#### ABSTRACT

The increasing demand for high performance and energy efficiency in Artificial Neural Networks (ANNs) and Deep Learning (DL) accelerators has driven a wide range of application-specific integrated circuits (ASICs). In recent years, this field has started to deviate from the conventional digital implementation of machine learning-based (ML) accelerators; instead, researchers have started to investigate implementation in the analog domain. This is due to two main reasons: (a) better performance, and (b) lower power consumption. Analog processing has become more efficient than its digital counterparts, especially for Deep Neural Networks (DNNs), partly because emerging analog memory technologies have enabled local storage and processing known as compute-in-memory (CIM), thereby reducing the

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amount of data movement between the memory and the processor. However, there are a lot of challenges in the analog domain approach, such as the lack of a capable commercially available non-volatile analog memory, and the analog domain is susceptible to variation and noise. Additionally, analog cores involve digital-to-analog converters (DACs) and analog-to-digital converters (ADCs), which consume up to 64% of total power consumption. An emerging trend has been to employ time-domain (TD) circuits to implement the multiply-accumulate (MAC) operation. TD cores require time-to-digital converters (TDCs) and digital-to-time converters (DTCs).

However, DTC and TDC can be more energy and area efficient than DAC and ADC. TD accelerators leverage both digital and analog features, thereby enabling energy-efficient computing and scaling with complementary metal–oxide– semiconductor (CMOS) technology. The performance of TD accelerators can be substantially improved if customdesigned analog delay cells, DTC, and TDC are used. This work reviews state-of-the-art TD accelerators and discusses system considerations and hardware implementations. Additionally, the work analyzes the energy and area efficiency of the TD architectures, including spatially unrolled (SU) and recursive (REC) architectures, for varying input resolutions and network sizes to provide insight for designers into how to choose the appropriate TD approach for a particular application. Furthermore, it discusses our implemented scalable SU-TD accelerator synthesized in 65 nm CMOS technology with an efficient DTC circuit that utilizes a laddered inverter (LI) circuit that consumes  $3 \times$  less power than the inverter-based DTC and achieves 116 TOPS/W. Finally, we discuss the limitations of time-domain computation and future work.

## <span id="page-10-0"></span>**Introduction to Efficient Computing**

#### <span id="page-10-1"></span>**1.1 Introduction**

Deep Neural Networks (DNNs) have become the cornerstone for modern artificial intelligence (AI) applications due to the unprecedented achieved accuracy in image classification [\[47\]](#page-24-0), [\[76\]](#page-27-0), object recognition/detection [\[35\]](#page-23-0), [\[77\]](#page-28-0), [\[82\]](#page-28-1), speech recognition [\[21\]](#page-21-0), [\[22\]](#page-21-1), [\[24\]](#page-21-2), [\[40\]](#page-23-1), [\[71\]](#page-27-1), [\[74\]](#page-27-2), [\[86\]](#page-29-0), game playing [\[17\]](#page-20-0), [\[65\]](#page-26-0), [\[83\]](#page-28-2), [\[84\]](#page-28-3), healthcare [\[6\]](#page-19-0), [\[30\]](#page-22-0), [\[99\]](#page-30-0), [\[102\]](#page-30-1), [\[104\]](#page-31-0), and robotics [\[51\]](#page-24-1), [\[73\]](#page-27-3), [\[81\]](#page-28-4), [\[103\]](#page-30-2). As DNNs require significant computational resources, energy, and memory bandwidth to process huge amounts of data with small latency and high accuracy [\[88\]](#page-29-1), they are typically implemented on the cloud using GPUs. Moving DNNs, however, out of the cloud into the edge devices provides key benefits, including improving privacy in some applications, such as healthcare, and reducing latency, which is critical in modern applications like autonomous driving.

Over the last 50 years, Moore's law and Dennard scaling have helped build faster, smaller, and energy-efficient transistors, but this trend has slowed down during the last decade due to the physical limits of the transistors [\[25\]](#page-21-3), [\[96\]](#page-29-2). To overcome this limitation, various levels of research have built specialized computing hardware that can deliver high performance with high energy efficiency. Digital accelerators can

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be custom-made specifically for DNNs and thus can provide higher throughput, shorter latency, lower energy, and higher area efficiency [\[9\]](#page-19-1), [\[18\]](#page-20-1), [\[19\]](#page-20-2), [\[23\]](#page-21-4), [\[26\]](#page-21-5), [\[29\]](#page-22-1), [\[43\]](#page-23-2), [\[55\]](#page-25-0), [\[66\]](#page-26-1), [\[67\]](#page-26-2), [\[87\]](#page-29-3), [\[88\]](#page-29-1), [\[92\]](#page-29-4), [\[94\]](#page-29-5). Although digital accelerators provide better performance compared to GPUs, digital systems (including both GPUs and digital accelerators) are fundamentally limited in handling big data efficiently due to the separation of logic and memory (referred to as von Neumann bottleneck). Consequently, the system bandwidth is limited by the speed of accessing the data in the memory. Moreover, memory access requires at least 10x more energy/delay compared to the multiply-accumulate (MAC) operation [\[41\]](#page-23-3), [\[88\]](#page-29-1). Hence, data movement in GPUs and digital accelerators dominates energy consumption and bandwidth.

To overcome the fundamental challenges in digital systems, analog and mixed-signal hardware accelerators have been explored to build artificial neural networks (ANNs) that can outperform the digital-based ones by several orders of magnitudes in energy efficiency, computation, and training time [\[11\]](#page-19-2), [\[12\]](#page-19-3), [\[16\]](#page-20-3), [\[27\]](#page-21-6), [\[28\]](#page-22-2), [\[32\]](#page-22-3), [\[45\]](#page-24-2), [\[49\]](#page-24-3), [\[54\]](#page-25-1), [\[58\]](#page-25-2), [\[75\]](#page-27-4), [\[89\]](#page-29-6), [\[91\]](#page-29-7), [\[98\]](#page-30-3), [\[100\]](#page-30-4). Analog computations promise simplicity and energy efficiency with real-time parallel processing and learning. Analog processing has become more efficient than the digital counterparts, especially for DNNs, partly because emerging analog memory technologies have enabled local storage and processing as shown in Figure [1.1\(](#page-13-1)c), thereby reducing the amount of data movement between the memory and the processor. Besides, the MAC operations can be performed more efficiently in the analog domain. An ultimate example of analog computation is the human brain, which can perform more than 1016 operations/second while consuming 20 Watts [\[61\]](#page-26-3). Although analog computation is efficient in terms of energy and area [\[91\]](#page-29-7), [\[98\]](#page-30-3), it has limited accuracy and technology scaling [\[7\]](#page-19-4). Additionally, the need for Analog-to-Digital converters (ADCs) and Digital-to-Analog converters (DACs) limits the efficiency and scalability of the analog cores.

An emerging trend is to utilize time-domain (TD) to perform MAC operations by representing the data as pulses with modulation, as depicted in Figure [1.1\(](#page-13-1)d) [\[3\]](#page-18-1), [\[7\]](#page-19-4), [\[20\]](#page-21-7), [\[31\]](#page-22-4), [\[56\]](#page-25-3), [\[64\]](#page-26-4), [\[79\]](#page-28-5). The goal is to perform the MAC operations in TD by producing proportional delays to inputs and weights. These delays are accumulated and then converted

#### 1.2. Background and Prior Work 5

back to digital. TD cores require time-to-digital converters (TDCs) and digital-to-time converters (DTCs). However, DTC and TDC can be more energy and area efficient than DAC and ADC, respectively [\[63\]](#page-26-5). Time-based accelerators can achieve superior performance while being energy efficient [\[2\]](#page-18-2), [\[7\]](#page-19-4), [\[20\]](#page-21-7), [\[31\]](#page-22-4), [\[56\]](#page-25-3), [\[64\]](#page-26-4), [\[79\]](#page-28-5). It has been shown that TD-ANN can achieve superior performance with excellent energy and hardware efficiency [\[2\]](#page-18-2), [\[7\]](#page-19-4), [\[20\]](#page-21-7), [\[31\]](#page-22-4), [\[56\]](#page-25-3), [\[64\]](#page-26-4), [\[79\]](#page-28-5). The digital approach has the best use of technology scaling, but it is not as efficient as the analog approach [\[7\]](#page-19-4), [\[91\]](#page-29-7), [\[98\]](#page-30-3). Time-based computation can take advantage of both approaches, analog and digital, as it is energy efficient and can be scaled with CMOS technology.

#### <span id="page-12-0"></span>**1.2 Background and Prior Work**

The concept of neural networks was inspired by the biological neural system and was first conceived in 1943 [\[60\]](#page-26-6). Fully connected DNNs (FC-DNN) consist of multiple layers, an input layer that matches the width of the input data, an output layer that depends on the specific inference task and hidden layers. Figure  $1.1(a)$  $1.1(a)$  shows a feedforward FC-DNN architecture that is based on MAC or vector-matrix multiplication (VMM), where a vector of  $n$  neuron excitations,  $x_i$ , is multiplied by a vector of weights,  $w_{ij}$ , generating a new vector of neuron excitations for the next layer,  $y_j$ , and then followed by a nonlinear function,  $f$ .

$$
y_i = f\left(\sum_i^n w_{ij} x_i\right). \tag{1.1}
$$

In the digital domain, Figure  $1.1(b)$  $1.1(b)$  shows how a GPU implements the MAC operations, by using a large number of Arithmetic Logic Units (ALU) with the help of memory (DRAM) that stores the weights. Figure [1.1\(](#page-13-1)c) shows an example of analog domain implementation where memory technologies have enabled local storage and processing. Figure [1.1\(](#page-13-1)d) represents the basic implementation of TD neuron. As depicted in the figure, a chain of variable delay elements are cascaded where each element has a delay value that depends on the dot product between the corresponding input and weight. An input pulse is applied at

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<span id="page-13-1"></span>

**Figure 1.1:** (a) DNN with basic mathematical operations, (b) GPU architecture, (c) analog computation, (d) time-domain computation.

the first element where the output pulse width will eventually represent the MAC result for the neuron.

#### <span id="page-13-0"></span>**1.3 Introduction to Analog Computing**

To overcome the fundamental challenges in digital systems, analog and mixed-signal hardware accelerators have been explored to build artificial neural networks (ANNs) that can outperform the digital-based ones by several orders of magnitudes in energy efficiency, computation, and training time  $[11]$ ,  $[12]$ ,  $[16]$ ,  $[27]$ ,  $[28]$ . Analog computations promise simplicity and energy efficiency with real-time parallel processing and learning. Analog processing has become more efficient than its digital counterparts, especially for DNNs, partly because emerging analog memory technologies have enabled local storage and processing, thereby reducing the amount of data movement between the memory and the processor. Analog computing provides the ultimate in-memory computing (IMC) as it can be implemented in crossbar architecture. Besides, the MAC operations can be performed more efficiently in the analog domain. An ultimate example of analog computation is the human brain, which can perform more than 1016 operations/second while consuming 20 Watts [\[61\]](#page-26-3). The 2018 IBM Summit, one of the world's fastest supercomputers, may have a computing capacity comparable to that of the human brain [\[48\]](#page-24-4), but it consumes 13 MegaWatts, with an area of two basketball courts. Hence, to explore the capabilities of future computing, the human brain can potentially offer design tricks to implement non-von Neumann architectures toward highly efficient and massively parallel computing platforms [\[62\]](#page-26-7). The advantages of analog computation are (a) its superior energy efficiency as it mitigates data

#### 1.3. Introduction to Analog Computing T

movement and memory access for the neural network weights, and (b) its extremely high throughput as the current passes through the PEs in every column of the crossbar to get the MAC output.

#### **1.3.1 Hardware Implementation of Analog Computation**

Analog hardware accelerators utilize crossbar-based architectures and emerging non-volatile memories (NVM), such as Resistive RAM (RRAM) [\[5\]](#page-19-5), [\[10\]](#page-19-6), [\[15\]](#page-20-4), [\[42\]](#page-23-4), [\[46\]](#page-24-5), [\[52\]](#page-24-6), [\[53\]](#page-25-4), [\[72\]](#page-27-5), [\[97\]](#page-30-5), Phase-Change RAM (PCRAM) [\[8\]](#page-19-7), [\[14\]](#page-20-5), [\[33\]](#page-22-5), [\[80\]](#page-28-6), [\[95\]](#page-29-8), and Magnetic RAM (MRAM) [\[13\]](#page-20-6), are commonly used to build DNN systems. The crossbar architecture has rows and columns, where the NVM memory resides at the intersection between each row and column. This enables local storage and processing in a highly parallel and energy-efficient manner [\[11\]](#page-19-2), [\[12\]](#page-19-3), [\[16\]](#page-20-3), [\[27\]](#page-21-6), [\[28\]](#page-22-2).

A key component in DNNs is the memory to store the value of the weights [\[44\]](#page-24-7). Analog memory technologies can be divided into two categories: charge-storage and non-charge-storage memories. Chargestorage memories depend on storing electric charges for an extended period of time. Floating-gate or embedded flash memory (eFM) is a NVM, charge-type memory that is used in DNNs [\[27\]](#page-21-6), [\[39\]](#page-23-5), [\[70\]](#page-27-6). eFM has a tunnel gate oxide at the channel interface, but due to the stringent requirement of long retention time, this tunnel oxide is already at its minimum thickness and is no longer scalable [\[13\]](#page-20-6). Furthermore, eFM requires high voltage pulses for programming and erasing, thereby potentially leading to high power consumption and long training times. Non-charge-storage memories are typically two-terminal, NVM devices, including RRAM, PCRAM, and MRAM.

#### **1.3.2 Limitations of Analog Accelerators**

In addition to the storage elements challenges in IMC architecture mentioned previously, analog accelerators are sensitive to noise, not like their digital counterpart which deals with two levels; 0 s and 1 s. The major sources of noise are thermal noise from electronic devices and quantization noise that comes from the crossbar interface circuits which are the data converters that convert the data from digital to analog and then from analog to digital [\[37\]](#page-23-6), [\[68\]](#page-26-8). The issue becomes more

#### 8 **Introduction to Efficient Computing**

challenging for higher precision as it is well known that the thermal noise is proportional to  $\sqrt{kT/C}$ , and thus to achieve an extra bit, the capacitance needs to be increased fourfold and as a result, the energy will be increased 4 times [\[68\]](#page-26-8). So it is very challenging to design a high-precision analog core while being more efficient than digital cores. It has been shown that analog accelerators can be more energy-efficient than digital for low-bit precision, i.e., below 6–7 bits, otherwise digital will outperform the analog core [\[37\]](#page-23-6), [\[68\]](#page-26-8), [\[69\]](#page-27-7), [\[78\]](#page-28-7), [\[93\]](#page-29-9).

In IMC architecture, the cost of accumulation operation is directly related to the conversion from analog to digital using an analog-todigital converter (ADC). One ADC can be used for each column at the crossbar architecture, or multiple columns can share a high-speed ADC by using the means of reusing and time-multiplexing. The energy per MAC operation can be expressed as follows [\[68\]](#page-26-8)

$$
E_{\rm MAC} = E_{\rm ADC}/N + E_{\rm CAP} + E_{\rm Logic}
$$
 (1.2)

Where  $E_{ADC}$  is the ADC's conversion energy, and N is the number of rows. *E*CAP and *E*Logic are the energy consumption due to the unit capacitances  $(C_u)$  and logic gates in each processing element. It has been shown that for higher bit precision (greater than 7 bits), the ADC energy will dominate [\[34\]](#page-22-6), [\[37\]](#page-23-6), [\[68\]](#page-26-8). Other works reported that the ADC consumes 64% of total energy in [\[59\]](#page-25-5), and 50% of total core power in [\[36\]](#page-23-7), which urges the need for energy and area-efficient ADC designs.

#### <span id="page-15-0"></span>**1.4 Digital vs. Analog vs. Time-Domain Computing**

The adaptable nature of the digital implementation allows for scalability using CMOS technology. However, due to data representation as a multibit digital vector, as the number of bits increases, so does the quantity of MAC units and operations. This leads to heightened dynamic switching capacitance, resulting in increased power consumption and additional area overhead [\[7\]](#page-19-4), [\[9\]](#page-19-1), [\[18\]](#page-20-1), [\[19\]](#page-20-2), [\[23\]](#page-21-4), [\[26\]](#page-21-5), [\[29\]](#page-22-1), [\[43\]](#page-23-2), [\[55\]](#page-25-0), [\[66\]](#page-26-1), [\[67\]](#page-26-2), [\[87\]](#page-29-3), [\[88\]](#page-29-1), [\[92\]](#page-29-4), [\[94\]](#page-29-5).

In the analog domain, data are depicted through continuously varying voltage signals. Various analog-based accelerators have been suggested to execute MAC operations by employing charge manipulation

#### 1.4. Digital vs. Analog vs. Time-Domain Computing 9

techniques and Analog-to-Digital Converters (ADCs) [\[11\]](#page-19-2), [\[12\]](#page-19-3), [\[16\]](#page-20-3), [\[27\]](#page-21-6), [\[28\]](#page-22-2), [\[32\]](#page-22-3), [\[45\]](#page-24-2), [\[49\]](#page-24-3), [\[54\]](#page-25-1), [\[58\]](#page-25-2), [\[75\]](#page-27-4), [\[89\]](#page-29-6), [\[91\]](#page-29-7), [\[98\]](#page-30-3), [\[100\]](#page-30-4). Analog methodologies execute MAC operations within the analog voltage domain utilizing a Static Random Access Memory (SRAM) array, capacitors, and data converters. In these methodologies, input pixel data are encoded either as a Pulse-Width Modulation (PWM) signal or a Pulse-Amplitude-Modulated (PAM) signal. The MAC operation is carried out by summing the read current of simultaneously accessed bit-cells. However, this approach is vulnerable to process variations, noise, bit-flips, and weak line corruption. Despite analog computations demonstrating efficiency in terms of energy  $\left($  OPS/W) and area  $\left($  OPS/mm<sup>2</sup> $\right)$ , they exhibit limited accuracy and technology scaling due to finite voltage headroom [\[7\]](#page-19-4).

In Time-Domain (TD) representation, data are depicted as pulses with variable widths or time differences in rising/falling edges, thereby generating variable delays. The TD methodology amalgamates the benefits of both digital and analog approaches; it can scale effectively with technology and offers energy-efficient computation. Furthermore, unlike analog-based computation, which necessitates an analog circuit design flow, TD circuits can employ the digital Integrated Circuit (IC) design flow, facilitating large-scale integration. Prior research indicates that TD cores can outperform digital implementations of Artificial Neural Networks (ANNs) only when the number of input bits is relatively low [\[2\]](#page-18-2), [\[7\]](#page-19-4). In Time-Domain (TD) Artificial Neural Networks (ANNs), calibration becomes necessary due to the analog nature of the delay signal, which is more susceptible to noise and process variation. Additionally, the TD approach necessitates the inclusion of additional components like time-to-digital converters (TDCs) and digital-to-time converters (DTCs). Nonetheless, DTCs and TDCs remain more energyand area-efficient compared to Digital-to-Analog Converters (DACs) and Analog-to-Digital Converters (ADCs) [\[63\]](#page-26-5). TD computing is particularly well-suited for applications requiring low resolution and stringent power constraints, such as edge devices. Phase-Domain (PD) ANN operates similarly to TD, but it employs phase shifts to execute the dot product [\[90\]](#page-29-10). The main issues are requiring multiple clock sources and

<span id="page-17-1"></span>10 **Introduction to Efficient Computing** 



**Table 1.1:** Comparing different accelerators

the dependence of the toggle activity on the input magnitude. Table [1.1](#page-17-1) summarizes the aforementioned approaches.

#### <span id="page-17-0"></span>**1.5 Motivation and Scope of the Study**

Due to the tremendous number of IoT applications and edge computing where stringent power constraints are required, the need for highly efficient ultra-low-power computing is essential. This work aims to explore and analyze energy-efficient accelerators for edge computing; specifically time-domain and mixed-signal domain cores. Analog computations offer outstanding energy efficiency with real-time parallel processing and learning. This is mainly due to the emerging analog memory technologies which have enabled local storage and processing. Although analog computation is efficient in terms of energy, it has limited accuracy and technology scaling [\[7\]](#page-19-4). Additionally, the need for average resolution (e.g., 8 bits) ADCs and DACs limits the efficiency and scalability of the analog cores. Reported works in the literature show that ADCs can contribute up to  $64\%$  of total energy consumption [\[59\]](#page-25-5), which makes it hard to compete against digital accelerators. An emerging trend is to utilize time-domain (TD) to perform MAC operations by representing the data as pulses with modulation, Time-based computation can take advantage of both approaches, analog and digital, as it is energy efficient and can be scaled with CMOS technology.

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- <span id="page-18-2"></span>[2] H. Al Maharmeh, N. J. Sarhan, C.-C. Hung, M. Ismail, and M. Alhawari, "Compute-in-time for deep neural network accelerators: Challenges and prospects," in *2020 IEEE 63rd International Midwest Symposium on Circuits and Systems (MWSCAS)*, pp. 990– 993, Springfield, MA, USA, 2020.
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